November 3, 2003

Working With Real Numbers
Must use approximations

 Infinite number of reals
 Finite number of bits

Floating Point
Fixed Point

Floating Point

Based on scientific notation

- Value = ±fraction * base ±exponent
- Base is a power of 2 (2 and 16 most common)
- Example: <u>IEEE-754</u>
 - Short (Used for Java's *float* type)
 - 32 bits: 1 fraction sign, 8 signed exponent, 23 fraction value
 - Long (Used for Java's *double* type)
 - 64 bits: 1 fraction sign, 11 signed exponent, 52 fraction value

Floating Point ALU

Parse operands

- Sign of fraction
- Value of fraction
 - IEEE-754: Restore hidden 1
- Exponent
- Align fractions
 - Shift value and adjust exponent.
- Perform calculation
- Normalize result
 - Fraction must be binary 01.xxx
 - Shift fraction and adjust exponent as necessary
- Construct floating point result
- Not to be implemented casually!

Fixed Point

- Fixed number of bits to the right of the binary point.
 - Integers (and unsigned integers) have zero bits to the right of the binary point.
- Hardware is the same as for signed and unsigned integers, no matter where the binary point is.
- Gives up dynamic range possible with floating-point.

Handel-C Fixed Point Library

See me for a copy of the manual.
fixed.hch and fixed.hcl are in the usual places.
Manual says you can encode arbitrary values,

Manual says you can encode arbitrary values but compilation fails if the real value cannot be represented precisely in the bit structure specified.

- For example 0.1₁₀ can not be used.
- Sample Code